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Day 1: Introduction to Functions
Aim: What is a function and how can we identify one?

## Introduction to Functions

A relation is a set of ordered pairs. A function is a relation in which each input value, or $x$-value, corresponds to exactly one output value, or $y$-value. A function or other relation can be represented as a set of ordered pairs in a table, as an equation, or by a graph.

The relationship represents a function if each input value is paired with only one output value.

Example 1: Determine whether each relationship is a function. Justify.
a:

| Input | Output |
| :---: | :---: |
| 5 | 7 |
| 10 | 6 |
| 15 | 15 |
| 20 | 2 |
| 25 | 15 |

b:

| $x$ | $y$ |
| :---: | :---: |
| 1 | 10 |
| 5 | 8 |
| 4 | 6 |
| 1 | 4 |
| 7 | 2 |

Example 2: Determine if the relationships below represent the graph a function? Justify.
Hours Studied and Exam Grade




## Graphing Linear Functions

When the graph of a relationship is a line, the equation is a linear equation. Since there is exactly one value of $y$ for each value of $x$, the relationship is a function. It is a linear function because its graph is a non-vertical line.

Example 3: Graph the function $\mathrm{y}=\mathrm{x}+3$
Step 1:Create a table.
Step 2: Pick input values (x) to find the output values (y).
Step 3: Graph the ordered pairs.

| $\mathbf{x}$ | $\mathbf{y}=\mathbf{x}+\mathbf{3}$ | $\mathbf{y}$ | $\mathbf{( x , y )}$ |
| :---: | :---: | :---: | :---: |
| $\mathbf{- 2}$ | $(-2)+3$ | 1 | $(-2,1)$ |
| $\mathbf{- 1}$ |  |  |  |
| $\mathbf{0}$ |  |  |  |
| $\mathbf{1}$ |  |  |  |
| $\mathbf{2}$ |  |  |  |



* A solution to the function is any point that lies on the line.
$\rightarrow$ Is $(-4,-1)$ a solution for this linear function? Justify.
$\rightarrow$ Is $(10,15)$ a solution for this linear function? Justify algebraically.


## Examples:

1. Complete the table and graph the function $y=-3 x+1$.

| $\mathbf{x}$ | $\mathbf{y}=-\mathbf{3 x}+\mathbf{1}$ | $\mathbf{y}$ | $(\mathbf{x}, \mathbf{y})$ |
| :---: | :--- | :--- | :--- |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |


2. Is $(-12,35)$ a solution to the previous linear function? Justify.
3. Tell whether each relationship is a function. Justify.
a:

| Input | Output |
| :---: | :---: |
| 1 | 6 |
| 2 | 7 |
| 3 | 7 |
| 4 | 6 |

b:

| $x$ | $y$ |
| :---: | :---: |
| -1 | 14 |
| 0 | 15 |
| 1 | 16 |
| -1 | 17 |

c: $\quad\{(2,1),(4,2),(6,3)\}$

## On your own!

(\#1-2) Determine whether each relationship is a function. Explain.
1.

| Input | Output |
| :---: | :---: |
| 52 | 53 |
| 24 | 24 |
| 32 | 32 |
| 17 | 17 |
| 45 | 45 |

2. 

| $\mathbf{x}$ | $\mathbf{y}$ |
| :---: | :---: |
| 14 | 52 |
| 8 | 21 |
| 27 | 16 |
| 36 | 25 |
| 8 | 34 |

3. Which of the following graphs represent a function? Justify your answer.

4. Which set of ordered pairs represent a function?
a: $\quad(-2,1),(0,1),(1,-2),(3,4)$
b: $\quad(-1,5),(-2,3),(-2,1),(-3,-1)$
c: $\quad(12,36),(9,27),(-6,30),(9,18)$
d: $\quad(3,17),(-2,11),(1,8),(3,5)$
5. Which table does not represent a function?
a:

| $\boldsymbol{x}$ | 7 | 8 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | 7 | 14 | 21 | 28 | 35 |

c:

| $\boldsymbol{x}$ | -8 | -4 | 0 | 4 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | 2 | 0 | -1 | -3 | -5 |

d:

| $\boldsymbol{x}$ | -10 | -5 | 0 | 5 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | 5 | 5 | 5 | 5 | 5 |

6. Is the relationship in the graph a function? Justify.

## Weights and Shipping Costs


7. Given the function $\mathbf{y}=\mathbf{- 2 x}+\mathbf{1}$, is $(-13,27)$ a solution to this function? Justify.

