


Intro to Functions

A relation is a set of ordered pairs. A **function** is a relation in which each input value, or x-value, corresponds to exactly one output value, or y-value. A function or other relation can be represented as a set of ordered pairs in a table, as an equation, or by a graph.

 **The relationship represents a function if each input value is paired with only one output value.**
* x can't repeat *

Example 1: Determine whether each relationship is a function. Justify.

a:

Input	Output
5	7
10	6
15	15
20	2
25	15

Yes, this is a function
b/c no x values (input)
repeat.

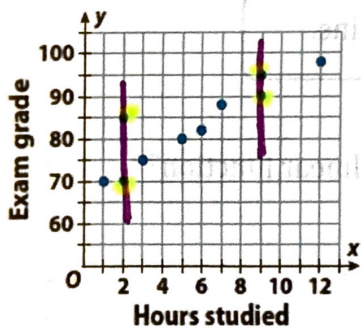
b:

x	y
1	10
5	8
4	6
1	4
7	2

No, this is NOT a
function b/c an x
value repeats.
1 (input) has more than 1
output.

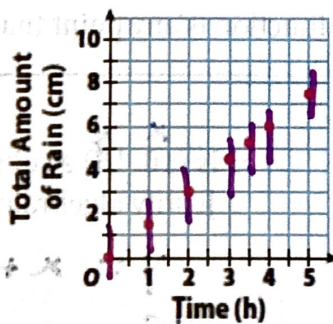
Example 2: Determine if the relationships below represent the graph a function? Justify.

Hours Studied and Exam Grade

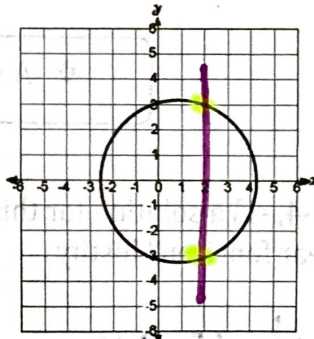


NOT a function
does NOT pass
VLT

Heavy Rainfall



This is a function.
It passes VLT.



NOT a function
does NOT pass
VLT

❖ **VERTICAL LINE TEST:** If the line hits the graph more than once, it is not a function.

Graphing Linear Functions

When the graph of a relationship is a **line**, the equation is a **linear equation**. Since there is exactly one value of y for each value of x , the relationship is a **function**. It is a **linear function** because its graph is a non-vertical line.

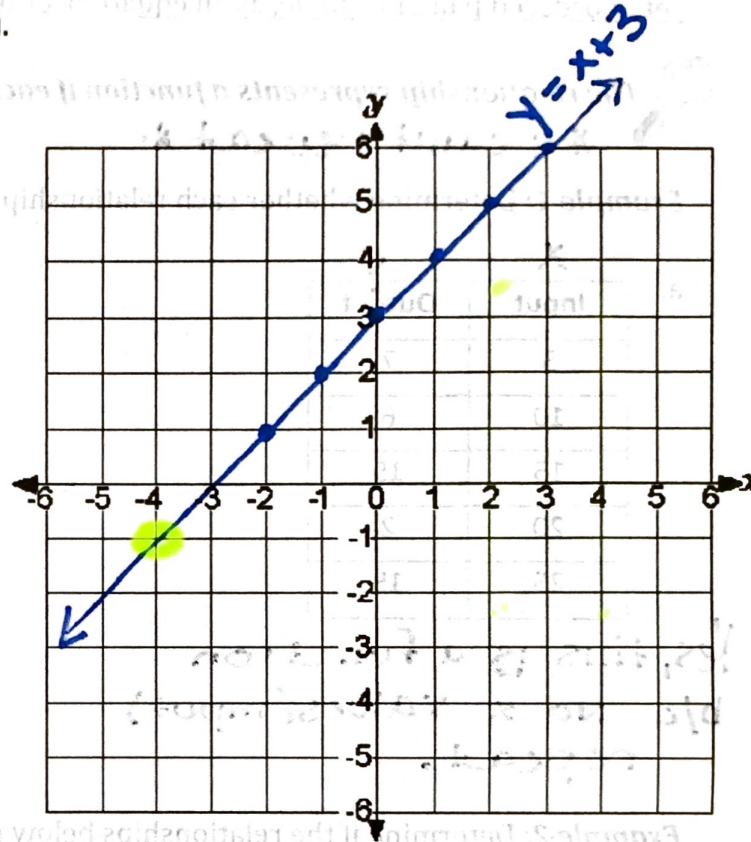
Example 3: Graph the function $y = x + 3$

Step 1: Create a table.

Step 2: Pick input values (x) to find the output values (y).

Step 3: Graph the ordered pairs.

x	$y = x + 3$	y	(x, y)
-2	$(-2) + 3$	1	$(-2, 1)$
-1	$(-1) + 3$	2	$(-1, 2)$
0	$(0) + 3$	3	$(0, 3)$
1	$(1) + 3$	4	$(1, 4)$
2	$(2) + 3$	5	$(2, 5)$



❖ A **solution** to the function is any point that lies on the line.

→ Is $(-4, -1)$ a solution for this linear function? Justify.

Yes, it is on the line.

→ Is $(10, 15)$ a solution for this linear function? Justify algebraically.

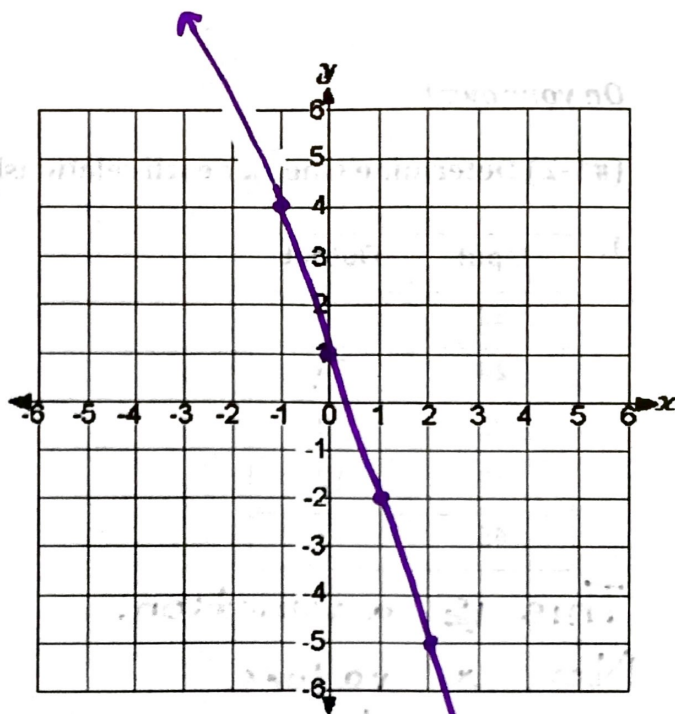
$$\begin{aligned}y &= x + 3 \\15 &= (10) + 3 \\15 &\neq 13\end{aligned}$$

Not a solution.

Examples:

1. Complete the table and graph the function $y = -3x + 1$.

x	$y = -3x + 1$	y	(x, y)
-2	$-3(-2) + 1$	7	(-2, 7)
-1	$-3(-1) + 1$	4	(-1, 4)
0	$-3(0) + 1$	1	(0, 1)
1	$-3(1) + 1$	-2	(1, -2)
2	$-3(2) + 1$	-5	(2, -5)



2. Is $(-12, 35)$ a solution to the previous linear function? Justify.

$$y = -3x + 1$$

$$35 = -3(-12) + 1$$

$$35 = 36 + 1$$

$$35 \neq 37$$

Not a solution.

$$y = -3x + 1$$

3. Tell whether each relationship is a function. Justify.

a:

Input	Output
1	6
2	7
3	7
4	6

This is a function.

No x values repeat.

b:

x	y
-1	14
0	15
1	16
-1	17

Not a function.

A value (-1) repeats.

c: $\{(2, 1), (4, 2), (6, 3)\}$

This is a function.

No x values repeat.